



$B_{(s)}^0 \rightarrow h^+ h'^-$ prospects at LHCb

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Outline



- ◆ **$B \rightarrow h^+ h'^-$ channels and U-spin symmetric modes**
- ◆ **Event selection**
- ◆ **Sensitivity on direct and mixing induced CP violation parameters**
- ◆ **Extraction of the γ angle of the unitarity triangle**
- ◆ **Conclusions**



Why $B \rightarrow h^+ h'^-$ decays interesting?



- ◆ **Since the original CLEO measurement that $BR(B_d \rightarrow K^+ \pi^-)$ is ~ 4 times larger than $BR(B_d \rightarrow \pi^+ \pi^-)$, it is well known that penguin diagrams cannot be neglected in the two-body B-decay amplitudes**
 - This fact complicates considerably the extraction of CKM phases from these decays
 - However, a possibility to eliminate unknown hadronic quantities relies in exploiting flavour symmetries, e.g. combining the measurements from U-spin related decay modes
- ◆ **This way, the presence of penguins can be transformed from a problem to an opportunity**
 - New Physics contributions might show up inside the loops of the penguin diagrams, and CKM quantities extracted from these modes can differ from the ones calculated from tree-level modes, which are basically unaffected from NP

U-spin ($d \leftrightarrow s$ quark exchange) symmetric modes

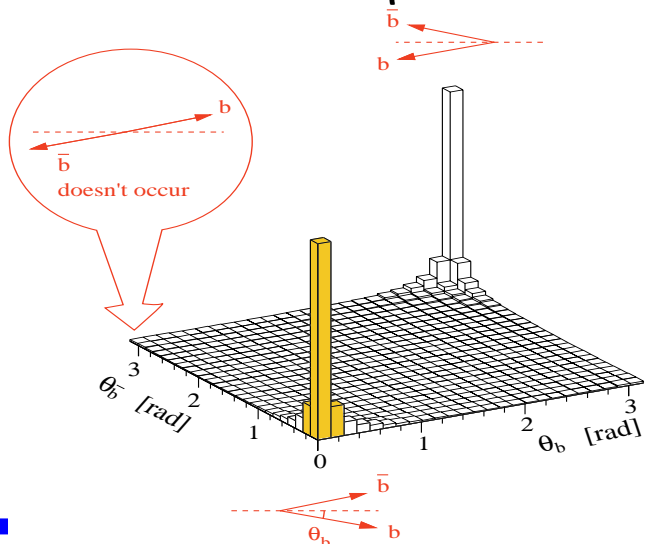
$B_d \rightarrow \pi^+\pi^-$ $T+P+P_{EW}^C+PA+E$	\longleftrightarrow	$B_s \rightarrow K^+K^-$ $T+P+P_{EW}^C+PA+E$
$B_d \rightarrow \pi^+\pi^-$ $T+P+P_{EW}^C+PA+E$	\longleftrightarrow	$B_s \rightarrow \pi^+K^-$ $T+P+P_{EW}^C$
$B_s \rightarrow K^+K^-$ $T+P+P_{EW}^C+PA+E$	\longleftrightarrow	$B_d \rightarrow K^+\pi^-$ $T+P+P_{EW}^C$

T: tree
P: penguin
 P_{EW}^C : colour suppressed electroweak penguin
PA: penguin annihilation
E: exchange

- Not all exactly U-spin symmetric, **E** and **PA** contributions missing from flavour specific decays
- E** and **PA** contributions expected to be relatively small, and can be experimentally probed by measuring the still unobserved $B_s \rightarrow \pi^+\pi^-$ and $B_d \rightarrow K^+K^-$ branching ratios ($BR \sim 10^{-8}$)

B → h⁺h^{'-} events produced at LHCb

- ◆ Large beauty production cross section expected at 14 TeV p-p collisions
 - All b-hadron species produced
- ◆ B hadrons are produced very likely with a small relative angle and in the very forward (backward) region
 - LHCb uses just the forward direction $1.8 < \eta < 4.9$



$B^+, B_d^0, B_s^0, B_c, \Lambda_b, \dots$
 ~40% ~40% ~10% ~10%

$\sigma_{b\bar{b}} \approx 500 \mu\text{b}$ $\frac{\sigma_{b\bar{b}}}{\sigma_{inelastic}} \approx 0.006$

$\sigma_{inelastic} \approx 80 \text{ mb}$ $\sigma_{inelastic}$

- ◆ At the nominal LHCb luminosity $\mathcal{L} = 2 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1}$ about 10^{12} B events are produced in 10^7 s
 - B → h⁺h^{'-} channels have typical branching ratios in the range $10^{-5} - 10^{-6}$
 - Millions of such events produced per year!



Event simulation

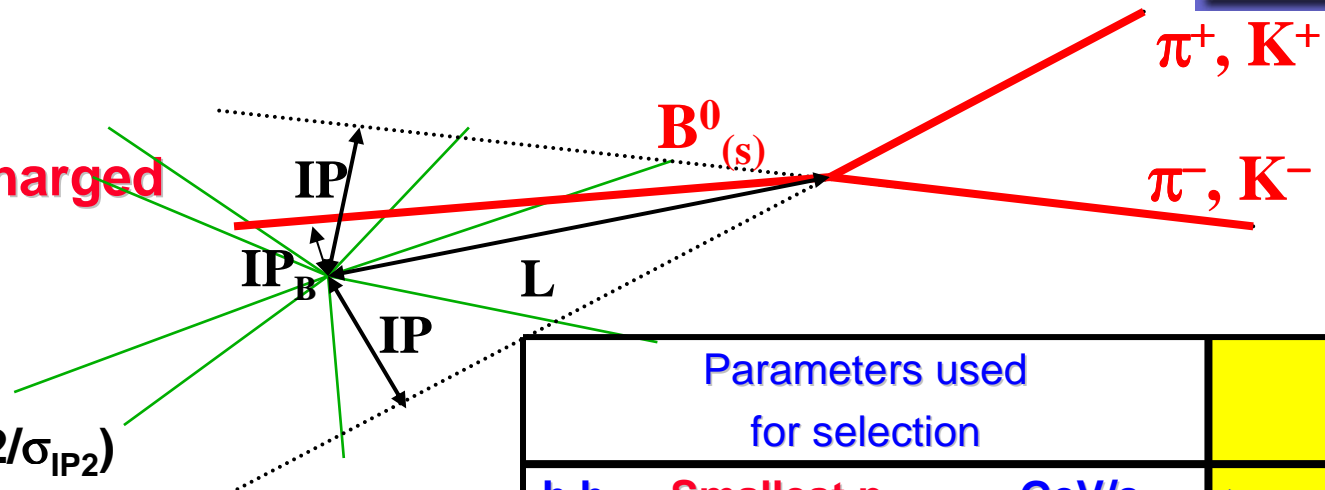


- ◆ **Event generation using Pythia 6.3 with dedicated LHCb tuning**
- ◆ **Full GEANT4 simulation and Pattern Recognition**
- ◆ **Problem: how to estimate combinatorial background-to-signal ratios before data comes?**
 - **Expected beauty production cross section is about 100 times less than visible cross section in the detector (~ 0.5 mb vs ~ 65 mb), and branching ratios of interest at 10^{-5} - 10^{-6}**
 - **The number of minimum bias events equivalent to signal events necessary to be generated and processed through GEANT4 is out of reach**
- ◆ **In order to study the combinatorial background we make the reasonable assumption that the dominant source comes from beauty events, thus reducing by a factor 100 the number of simulated events**
 - **Still a computing challenge, but affordable with currently available resources on the LCG**
- ◆ **For this study about 300k signal events and 27M inclusive beauty events have been used**

B → h⁺h^{'-} selection cuts

◆ For each pair of charged tracks we cut on

- max (p_{T1}, p_{T2})
- min (p_{T1}, p_{T2})
- max ($IP1/\sigma_{IP1}, IP2/\sigma_{IP2}$)
- min ($IP1/\sigma_{IP1}, IP2/\sigma_{IP2}$)
- χ^2 of common vertex

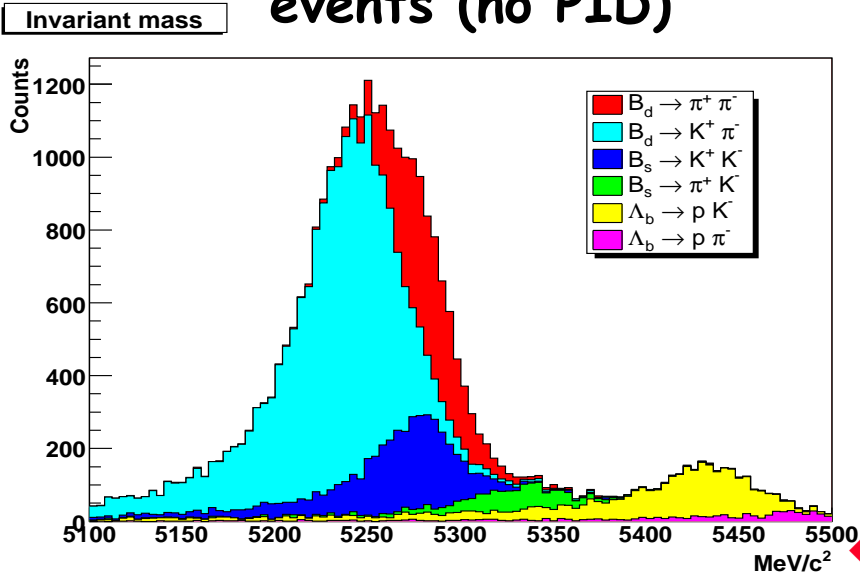


◆ Then, the B candidate is selected with cuts on

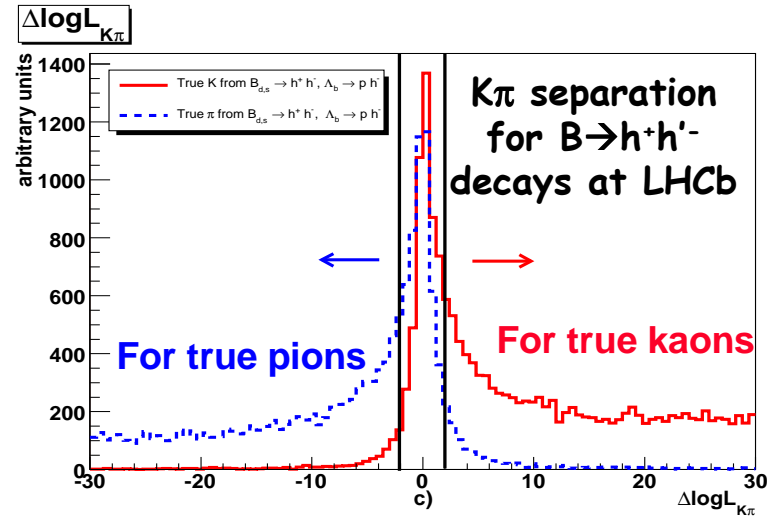
- ◆ p_T
- ◆ IP/σ_{IP}
- ◆ L/σ_L

Parameters used for selection			
h,h	Smallest p_t	GeV/c	> 1
h,h	largest p_t	GeV/c	> 3
h,h	smallest IP/σ_{IP}		> 6
h,h	largest IP/σ_{IP}		> 12
h, h	vertex fit χ^2		< 5
B	p_t	GeV/c	> 1
B	IP/σ_{IP}		< 2.5
B	L/σ_L		> 18

Invariant mass of selected events (no PID)



◆ PID discriminants built as difference between log likelihoods of particle hypotheses

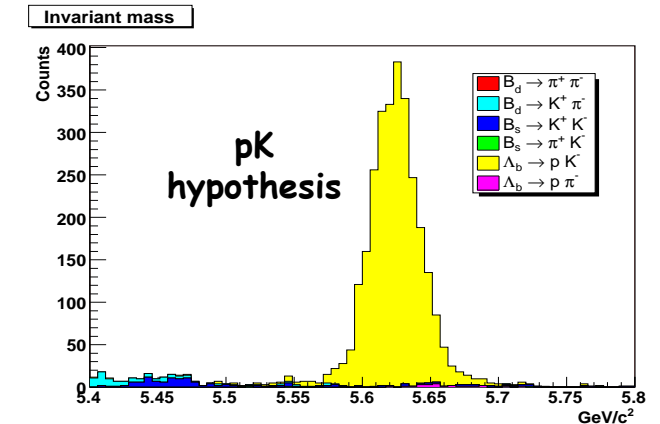
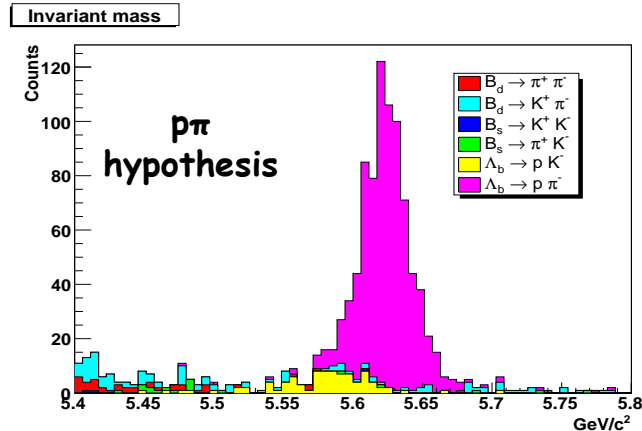
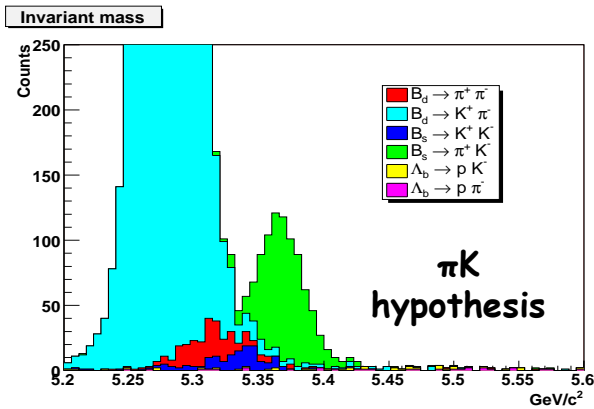
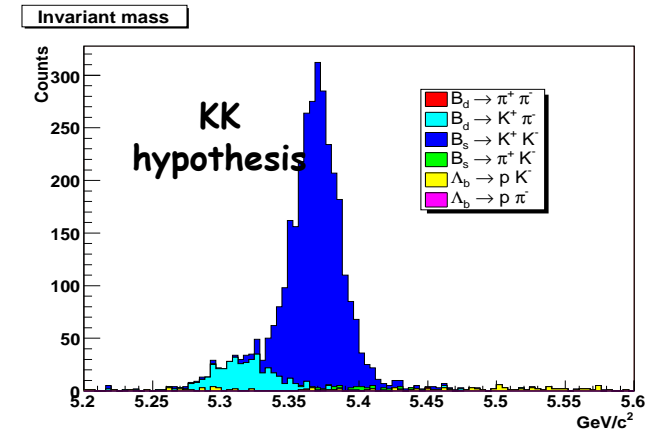
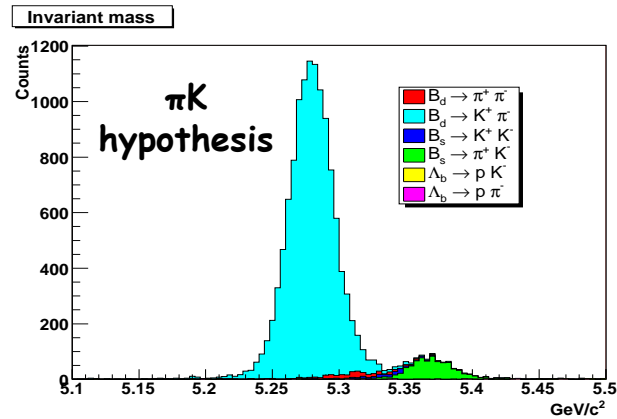
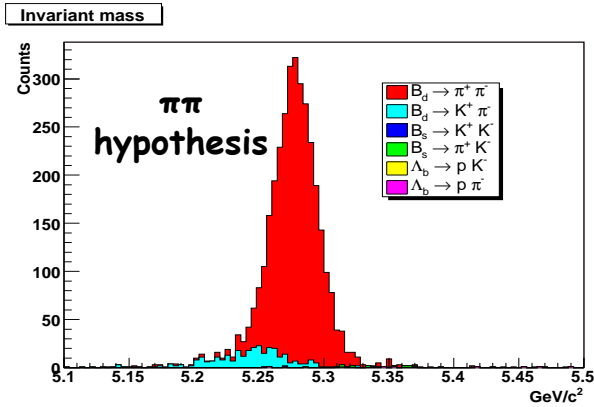


◆ Efficient hadron PID crucial for the $B \rightarrow h^+ h'^-$ channels

Channel	BR $\times 10^6$	
$B^0 \rightarrow \pi^+ \pi^-$	4.8	measured
$B^0 \rightarrow K^+ \pi^-$	18.5	measured
$B_s^0 \rightarrow \pi^+ K^-$	4.8	assumed
$B_s^0 \rightarrow K^+ K^-$	18.5	assumed
$\Lambda_b \rightarrow \pi^- p$	4.8	assumed
$\Lambda_b \rightarrow K^- p$	18.5	assumed

◆ Calibration of K/ π PID on data will be performed using the $D^{*+} \rightarrow D^0 \pi^+$, $D^0 \rightarrow K^+ \pi^-$ decay chain

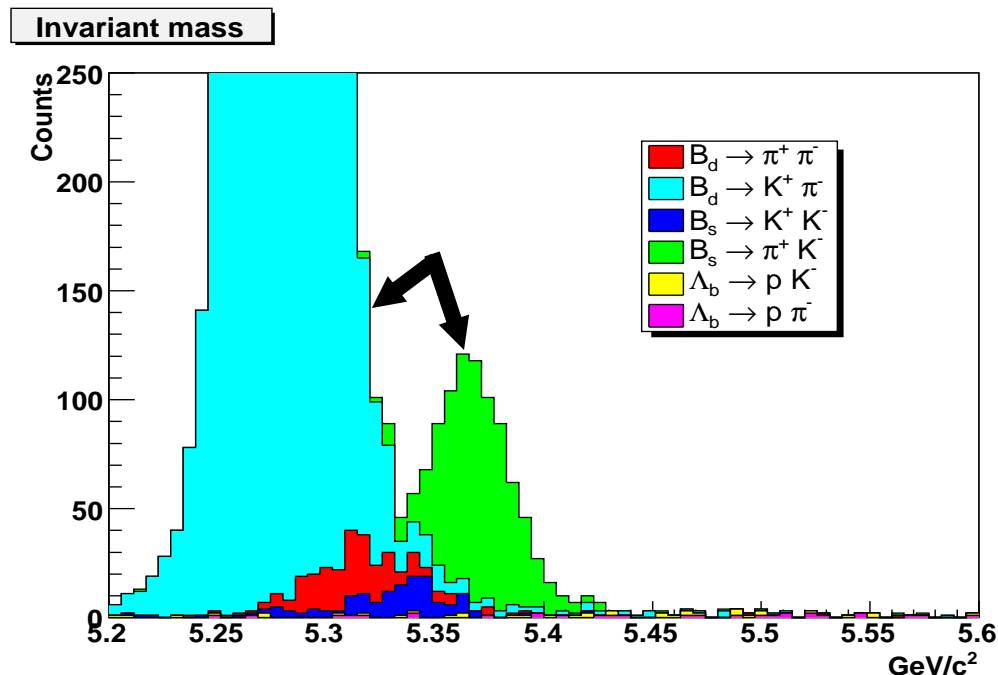
- Large "PID unbiased" samples of such D^* decays will be acquired with dedicated D^* trigger chain (300 Hz bandwidth) - see talk by Raluca Muresan



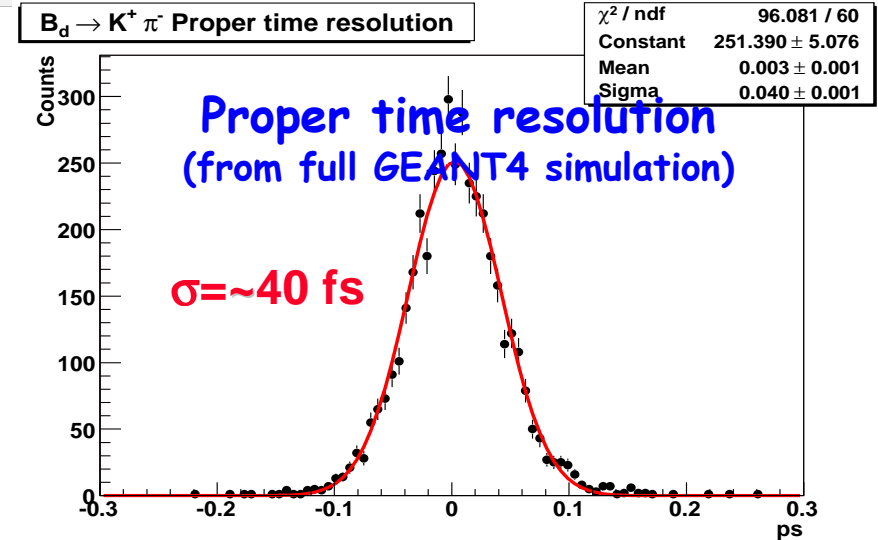
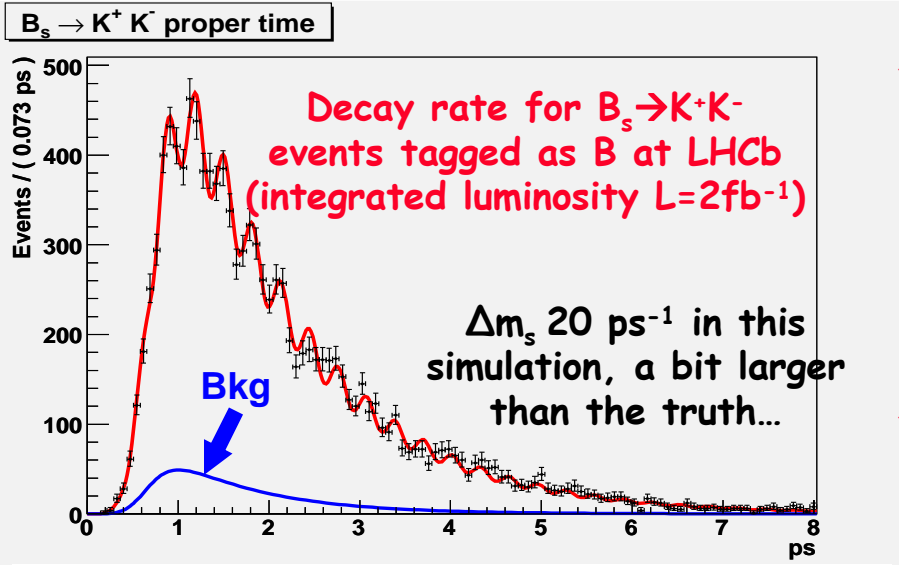
- ◆ Every h^+h^- channel is potentially a background for the other channels...
- ◆ ...but impressive performance of RICH systems allows to select very clean samples

Importance of good mass resolution

- ◆ Discrimination of $B_s \rightarrow \pi^+ K^-$ from $B_d \rightarrow K^- \pi^+$ must rely on mass resolution only since they share exactly the same signature
 - $B_d \rightarrow K^- \pi^+$ about 16 more abundant
 - 4 times larger branching fraction, 4 times large hadronization fraction



Nominal mass resolution of $\sigma=16 \text{ MeV}/c^2$ allows for a clean separation between the two signals



◆ Excellent proper time resolution allows to perfectly resolve the fast B_s oscillations

- $\sigma_t = \sim 40 \text{ fs}$
 - almost 10 times less than the oscillation period actually

◆ Calibration of proper time resolution on data very important to achieve in order not to be dependent on MC imperfections

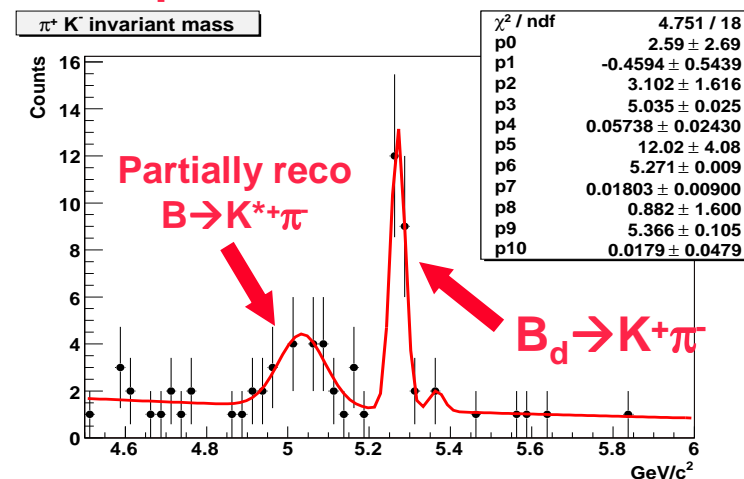
- will be done in LHCb by disentangling prompt $J/\psi \rightarrow \mu^+ \mu^-$ from non-prompt component from B decays
- The prompt component is affected just by the intrinsic resolution of the detector, hence can be used for calibration
- “Lifetime unbiased” prompt J/ψ events will be acquired with dedicated high-mass di-muon trigger (600 Hz bandwidth)

Selection performance summary

	$\epsilon_{tot} = \epsilon_{gen} \times \epsilon_{sel/gen} \times \epsilon_{trg/sel}$				BR 10^{-6}	Yield	B/S bb	B/S spec
	ϵ_{gen}	$\epsilon_{sel/gen}$	$\epsilon_{trg/sel}$	ϵ_{tot}				
$B_d^0 \rightarrow \pi^+ \pi^-$	34.9 ± 0.3	7.36 ± 0.13	36.3 ± 1.1	0.93 ± 0.03	4.8	35700	0.46	0.08
$B_d^0 \rightarrow K^+ \pi^-$	34.9 ± 0.3	7.21 ± 0.07	36.8 ± 0.6	0.93 ± 0.02	18.5	137600	0.14	0.02
$B_s^0 \rightarrow \pi^+ K^-$	34.8 ± 0.3	7.25 ± 0.30	40.6 ± 2.3	1.02 ± 0.06	4.8	9800	1.92	0.54
$B_s^0 \rightarrow K^+ K^-$	34.8 ± 0.3	7.11 ± 0.13	39.3 ± 1.2	0.97 ± 0.03	18.5	35900	< 0.06	0.08
$\Lambda_b \rightarrow p \pi^-$	34.6 ± 0.3	7.20 ± 0.26	38.3 ± 2.3	0.95 ± 0.06	4.8	9100	1.66	0.11
$\Lambda_b \rightarrow p K^-$	34.6 ± 0.3	6.80 ± 0.13	36.0 ± 1.1	0.86 ± 0.03	18.5	31800	< 0.08	0.02

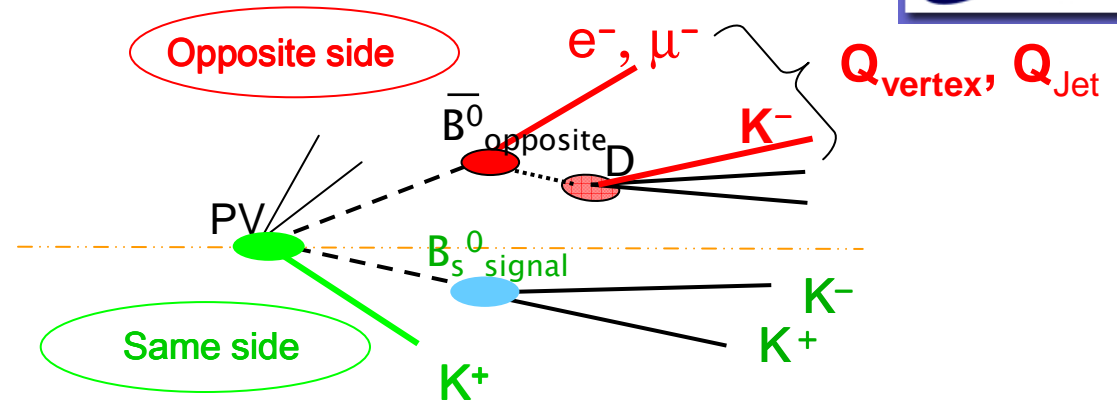
- ◆ Yields are calculated for an integrated luminosity of 2 fb^{-1}
 - 10^7 seconds at nominal LHCb luminosity
- ◆ Limited background-to-signal ratios
 - Both combinatorial and from the other $B \rightarrow h^+ h^-$ modes (due to wrong particle ID)
- ◆ Hundreds of thousands of $B \rightarrow h^+ h^-$ decays triggered, reconstructed and selected per year of running with high degree of purity!

πK spectrum selected from a sample of 27M $b\bar{b}$ MC events



Opposite side

- ◆ High p_T leptons
- ◆ K^\pm from $b \rightarrow c \rightarrow s$
- ◆ Vertex charge
- ◆ Jet charge



Same side

- ◆ Fragmentation K^\pm accompanying B_s
- ◆ π^\pm from $B^{**} \rightarrow B^{(*)}\pi^\pm$

$\epsilon D^2 = \epsilon(1-2\omega)^2$: tagging power

ϵ : tagging efficiency

ω : mistag probability

Tagging power in %

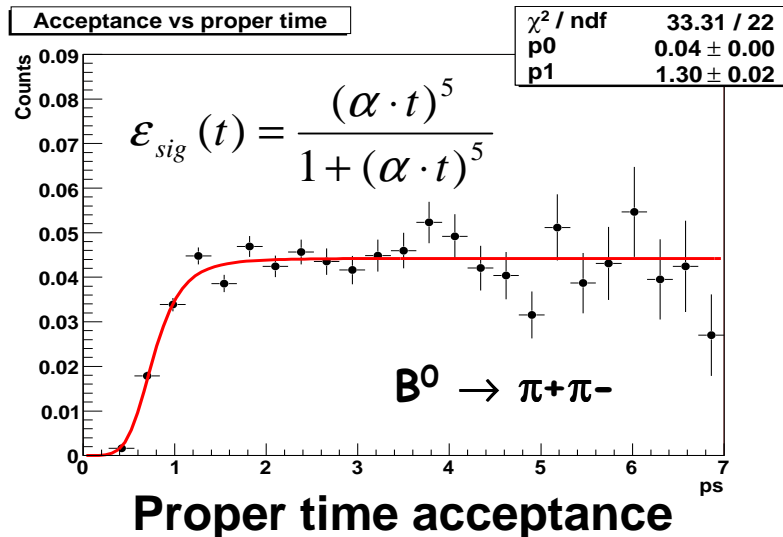
Tag	B_d	B_s
Muon	1.1	1.5
Electron	0.39	0.69
Kaon opp.side	2.1	2.3
Jet/ Vertex Charge	1.0	0.97
Same side π / K	0.73 (π)	3.5 (K)
Combined	5.05	9.5

Work in continuous progress.

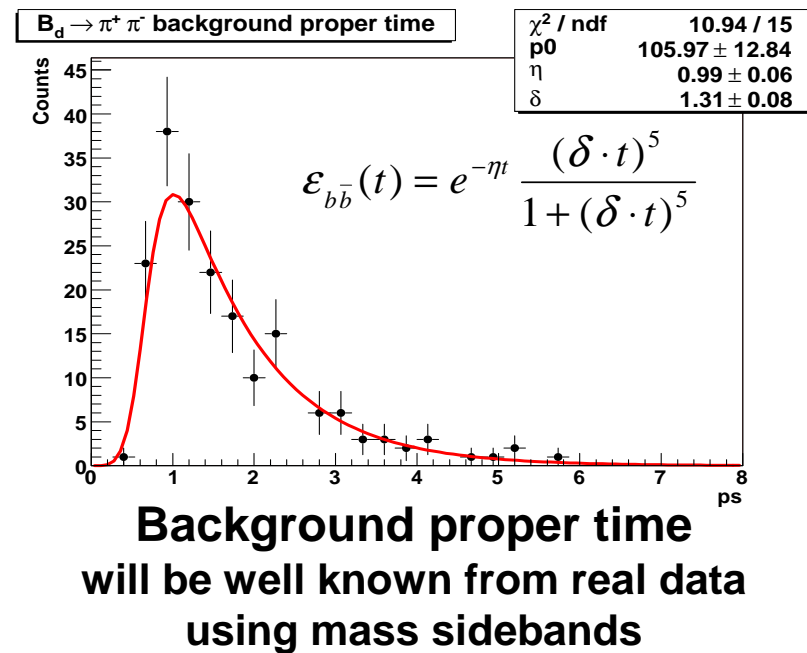
See talk on LHCb tagging by Hugo Ruiz

Toy MC generation for CP sensitivity studies

- ◆ A toy MC is used in order to generate large samples of signal and background events for estimating sensitivities on CP parameters from time dependent decay rate fits
- ◆ Signal samples generated simulating CP violation, proper time acceptance, proper time resolution and tagging
 - For each event the toy MC generates mass, proper time, tagging response, PID response according to the results from the full GEANT4 simulations
- ◆ Background mass and proper time spectra generated according to result from the full simulation



will be calibrated on real data using event by event acceptance functions – studies going on in LHCb



- ◆ **CP sensitivities are then estimated with an extended unbinned maximum likelihood fit to the toy MC sample**
 - The likelihood fit is performed simultaneously to all the $B \rightarrow hh$ channels, including tagged and untagged samples
 - The various channels and background are then separated each-other in the fit by means of the particle ID observables and invariant mass
- ◆ **In particular, the decay rate for $B_d \rightarrow \pi^+\pi^-$ and $B_s \rightarrow K^+K^-$ events tagged as B ($q=+1$) or \bar{B} ($q=-1$) entering the likelihood is given by**

$$F(t, q) = \left(1 + |\lambda_f|^2\right) \cosh \frac{\Delta\Gamma}{2} t - 2\Re(\lambda_f) \sinh \frac{\Delta\Gamma}{2} t + q \cdot (1 - 2\omega) \cdot \left[\left(1 - |\lambda_f|^2\right) \cos \Delta m t - 2\Im(\lambda_f) \sin \Delta m t \right]$$

$$\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f} \quad f = \pi^+\pi^-, K^+K^-$$

- ◆ **The usual C and S coefficients are related to λ_f by**

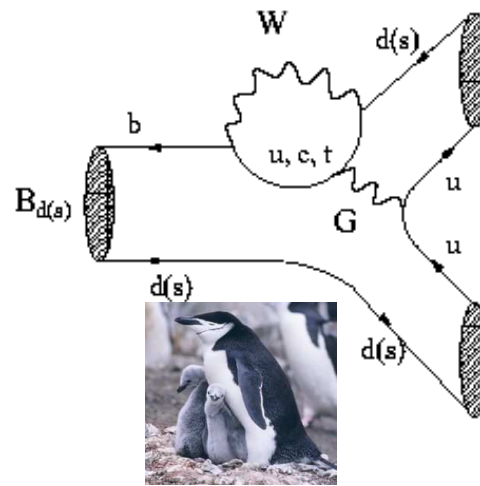
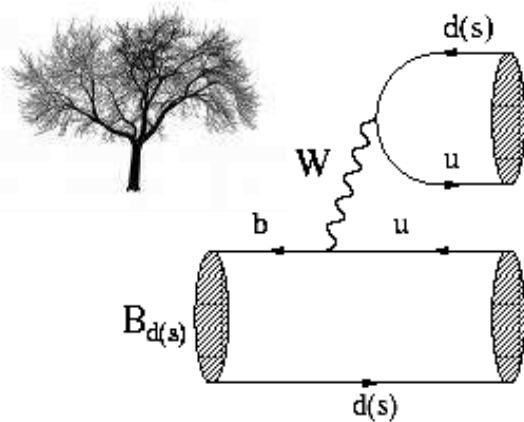
$$C_f = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2} \quad S_f = \frac{2\Im\lambda_f}{1 + |\lambda_f|^2}$$

- ◆ **LHCb can reach a sensitivity about 3 times better than the current world average in 10^7 s of running at nominal luminosity**

Fit results corresponding to Int. $L=2\text{fb}^{-1}$ (10^7 seconds at nominal LHCb luminosity)

	$B_d \rightarrow \pi^+\pi^-$	$B_s \rightarrow K^+K^-$
$\sigma(C)$	0.043 (0.10*)	0.042
$\sigma(S)$	0.037 (0.12*)	0.044
	$B_d \rightarrow K^+\pi^-$	$B_s \rightarrow \pi^+K^-$
$\sigma(A_{CP})$	0.003 (0.015*)	0.02

*Current world average



◆ Sensitivity to γ from the interference of T and P amplitudes

- d, d' : penguin-to-tree ratios
- θ, θ' : penguin-tree strong phase differences

$$A(B^0 \rightarrow \pi^+ \pi^-) = K(e^{i\gamma} - d e^{i\theta})$$

$$A(B_s^0 \rightarrow K^+ K^-) = \frac{\lambda}{1 - \lambda^2/2} K' \left(e^{i\gamma} + \frac{1 - \lambda^2}{\lambda^2} d' e^{i\theta'} \right) \leftarrow \text{Sensitivity to } \gamma \text{ doubly Cabibbo suppressed in this mode } \odot$$

- ◆ Relating by the U-spin symmetry the two amplitudes one gets $d=d'$ and $\theta=\theta'$

Using method and parametrization from
R. Fleischer, PLB 459 (1999) 306

Extraction of γ

$$C(B_d^0 \rightarrow \pi^+ \pi^-) = f_1(d, \vartheta, \gamma)$$

$$S(B_d^0 \rightarrow \pi^+ \pi^-) = f_2(d, \vartheta, \gamma, \phi_d)$$

$$C(B_s^0 \rightarrow K^+ K^-) = f_3(d', \vartheta', \gamma)$$

$$S(B_s^0 \rightarrow K^+ K^-) = f_4(d', \vartheta', \gamma, \phi_s)$$

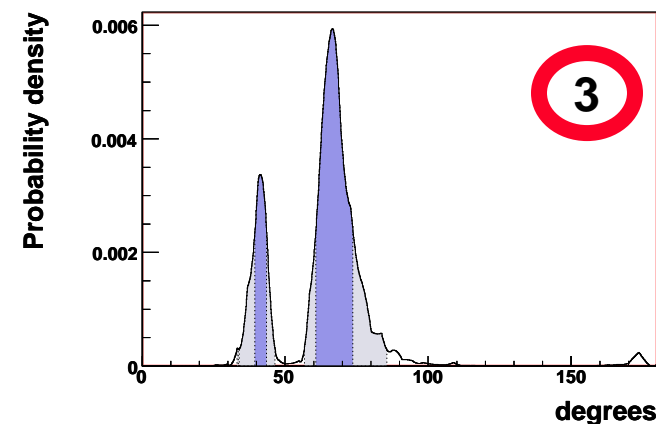
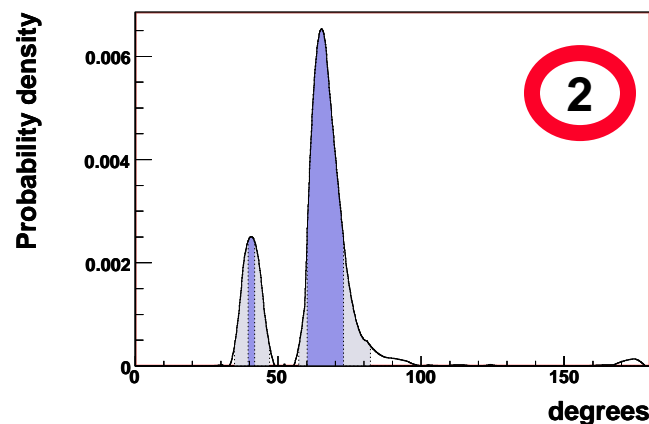
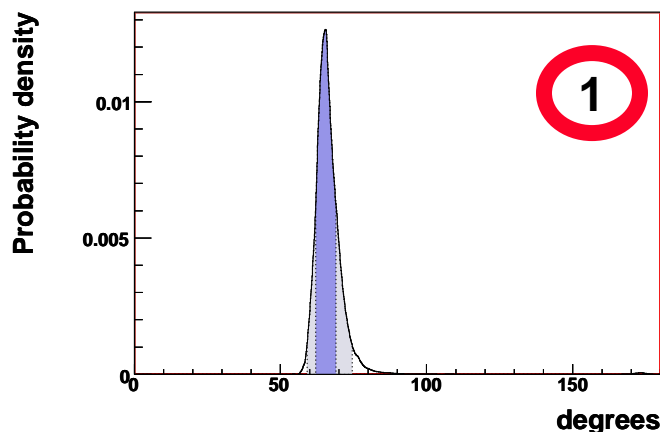
$$A_{CP}^{th}(\tau) = \frac{C \cdot \cos(\Delta M \cdot \tau) - S \cdot \sin(\Delta M \cdot \tau)}{\cosh\left(\frac{\Delta\Gamma}{2} \cdot \tau\right) - A_{\Delta\Gamma} \cdot \sinh\left(\frac{\Delta\Gamma}{2} \cdot \tau\right)}$$

Once the direct and mixing-induced CP-violating terms are measured, one has a system of **7 unknowns and 4 equations**

However, the mixing phase ϕ_d (ϕ_s) is (will be) measured from $B_d \rightarrow J/\psi K_S$ ($B_s \rightarrow J/\psi \phi$) \rightarrow **5 unknowns**

Finally, relying on U-spin symmetry one eliminates two further unknowns \rightarrow **3 unknowns, system over-constrained, γ can be extracted unambiguously**

- ◆ Extraction of γ performed with a Bayesian approach in 3 different scenarios (in this exercise $\gamma=65^\circ$ is assumed)
 - (1) Perfect U-spin symmetry
 - i.e. using the constraints $d=d'$ - $\theta = \theta'$
 - (2) Weaker assumption: perfect U-spin symmetry just for d, d'
 - $d=d'$ - no constraint on θ, θ'
 - (3) Even weaker: given U-spin breaking for d, d'
 - $\xi = d'/d = [0.8, 1.2]$ - no constraint on θ, θ'



Sensitivity ranging from $\sim 4^\circ$ in case of perfect U-spin assumed, to 7° - 10° partially releasing U-spin assumptions (but a secondary fake solution appears)



An exercise: using current world averages of $B_d \rightarrow \pi^+\pi^-$ and $B_d \rightarrow K^+\pi^-$ (not using LHCb results)



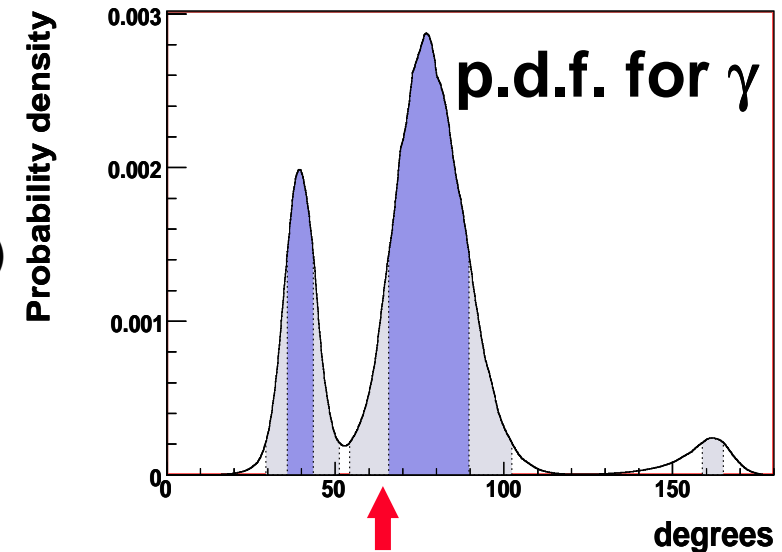
- ◆ Instead of using the $B_s \rightarrow K^+K^-$ one can make use of the $B_d \rightarrow K^+\pi^-$
 - It just differs for the spectator quark, but neglecting penguin annihilation and exchange diagrams which are not present in $B_d \rightarrow K^+\pi^-$
 - Assuming U-spin symmetry the cosine term of the time dependent asymmetry of $B_s \rightarrow K^+K^-$ is equal to the charge asymmetry of $B_d \rightarrow K^+\pi^-$, thus we can replace C_{KK} with $A_{K\pi}$
 - However one observable is missing, since S_{KK} is inaccessible, but still can solve system of constraints for γ

◆ Current world averages from HFAG

- $C_{\pi\pi} = -0.37 \pm 0.10$ (BaBar/Belle)
- $S_{\pi\pi} = -0.50 \pm 0.12$ (BaBar/Belle)
- $A_{K\pi} = -0.093 \pm 0.015$ (BaBar/Belle/CLEO/CDF)

◆ p.d.f. for γ obtained allowing for a U-spin breaking

- $\Delta\theta = \theta' - \theta = \pm 20^\circ$
- $\xi = d'/d = [0.8, 1.2]$



Unitarity Triangle fits expectation



Conclusions



- ◆ **LHCb will collect large samples of $B \rightarrow h^+ h'^-$ decays**
 - Its excellent vertexing and PID capabilities will allow to collect several hundreds of thousands of $B \rightarrow h^+ h'^-$ events with very high purity
- ◆ **The CP sensitivity reachable in 10^7 s of data taking at the nominal LHCb luminosity of $2 \cdot 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$ is estimated to be about 3 times better than the current world averages from the beauty factories and the Tevatron**
- ◆ **Besides the general interest of measuring CP violation for these channels, especially for the still unmeasured B_s decays, the $B \rightarrow h^+ h'^-$ modes can provide useful information to constrain the CKM angle γ**
 - This is accomplished by relating the B_d and B_s decay modes by means of the U-spin flavour symmetry
 - Even if the U-spin symmetry will result to be broken to some extent, we have shown how it is still possible to extract useful information on γ in scenarios where the U-spin breaking is taken into account
- ◆ **The extraction of γ from these decays can reveal contributions from New Physics inside the loops of the penguin diagrams, which contribute significantly to the $B \rightarrow h^+ h'^-$ modes**
 - γ obtained from these decay modes might thus be different from γ from tree level modes, such as $B \rightarrow DK$, which can be assumed to be basically free of New Physics contributions