

## BRITISH PHYSICS OLYMPIAD 2015-16

### A2 Challenge Sept/Oct 2015

### SOLUTIONS

#### Question 1

a.

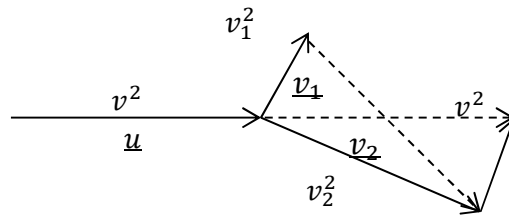
- i) Suitable diagram
- ii) Momentum calculation;  $1 \times 0.2 + 2 \times (-0.2) = 0$  i.e. total zero. *At rest*
- iii) At a point dividing the distance between the ships in the ratio 1:2 (closer to 2 tonne mass)  Zero
- iv) Before  $KE = \frac{1}{2}m_1 u_1^2 + \frac{1}{2}m_2 u_2^2 = \frac{1}{2}(1000 \times 0.2^2 + 2000 \times 0.1^2) = 30 \text{ J}$   ;  
 After - zero
- v) Suitable diagram  , Momentum calculation, total  $0.1 \text{ m s}^{-1}$  to the right  ;  
 position of c of m as before  ; 45 J before and 15 J after
- vi) Kinetic energies may differ according to frame of reference, but the loss remains the same   
 (As a de-brief point, it is instructive to demonstrate that the energy change,  $\Delta E = \frac{1}{2}(m_1 + m_2)(u_1 - u_2)^2$  is unaltered by a change to a frame of reference moving at speeds, which simply alters both  $u_1$  and  $u_2$  by the same amount,  $(u_1 - u_2) \rightarrow ((u_1 + \Delta u) - (u_2 + \Delta u))$  leaving the term  $(u_1 - u_2)$  unaltered.)

b.

- i) Momentum calculation to show appropriate velocities   
 Initial velocity,  $u$ . Final velocities  $v_1, v_2$ . Identical masses.  
 Mom cons.  $v_1 + v_2 = u$  (cancel through the  $m$ )  
 KE cons.  $v_1^2 + v_2^2 = u^2$  (cancel through by  $\frac{1}{2} m$ )  
 Algebra:  $(u - v_1)(u + v_1) = v_2^2$   
 And also  $(u - v_1) = v_2$  from the initial relation
- If  $v_2 \neq 0$  then can divide the two equations, to get  $(u + v_1) = v_2$ .  
 Now add  $(u + v_1) = v_2$  and  $(u - v_1) = v_2$  to obtain  $u = v_2$ , so that  $v_1 = 0$
- Note that if  $v_2 = 0$  then  $v_1 = u$  and momentum and KE are both conserved, but the particles do not actually collide.
- There are several other algebraic routes, including direct substitution for  $u$  say, giving  $v_1 \cdot v_2 = 0$ . So either  $v_1 = 0$  or  $v_2 = 0$ .

ii) Neutron comes to rest; proton ejected (as masses are virtually equal)

iii)



Let initial velocity be  $v$  and final velocities be  $\vec{v}_1$  and  $\vec{v}_2$ . Vector diagram to show  $m\vec{v}_1 + m\vec{v}_2 = m\vec{v}$   Elastic collision gives  $\frac{1}{2}mv_1^2 + \frac{1}{2}mv_2^2 = \frac{1}{2}mv^2$  so  $v_1^2 + v_2^2 = v^2$  implying (Pythagoras) that the momentum diagram is a right-angled triangle, proving the proposition.  **owwt**

Note: the analysis given in (i) is adaptable. Write cons. of mom as  $\vec{u} = \vec{v}_1 + \vec{v}_2$ . Squaring,  $u^2 = v_1^2 + v_2^2 + 2\vec{v}_1 \cdot \vec{v}_2$ . With the KE result,  $u^2 = v_1^2 + v_2^2$  clearly  $2\vec{v}_1 \cdot \vec{v}_2 = 0$

Thus  $v_1 = 0$  (linear collision as in (i)),  $v_2 = 0$  (no collision), or  $\cos \theta = 0 \Rightarrow \theta = \pi/2$

iv) Traces (such as cloud chamber tracks) seen to be perpendicular, when in the plane normal to the line of sight.

[16 marks]

### Question 2

a.

i) Initial volume  $1000 \text{ mm}^3$ ; final volume  $1000.40 \text{ mm}^3$   Increased (trivial)

ii) Bonds between atoms stretched, so a net volume increase reasonable **owtte**

iii) lateral strain =  $(-0.0003)$ ; longitudinal strain =  $0.001$ . So Poisson Ratio  $(-0.3)$  .

b.

i) Use binomial theorem or error theory ideas :

$V = lA$  so  $\frac{\delta V}{V} = \frac{\delta A}{A} + \frac{\delta l}{l}$ , from binomial or by differentiation.

Since  $\frac{\delta V}{V} = 0$  for rubber, and since  $\frac{\delta l}{l}$  increases by 2%, then  $\frac{\delta A}{A}$  reduces by 2%

ii)  $A = w^2$  so  $\frac{\delta A}{A} = 2 \frac{\delta w}{w}$ . Hence  $\frac{\delta w}{w}$  is reduced by 1%

iii) By inspection  $(-0.5)$

[6 marks]

### Question 3

a. i) Suitable *symmetrical* diagram

ii) Angle-sum of triangles gives  $Li$  for incident ray as  $(A+D)/2$    $Lr = A/2$

$$n = \frac{\sin((A+D)/2)}{\sin(A/2)} \quad \text{follows from Snell's Law} \quad \checkmark$$

i) For  $\sin \theta \approx \theta$  this reduces to  $n = \frac{(A+D)/2}{A/2}$   which re-arranges to  $D = (n - 1)A$

- b.
- i) Deviation =  $(n-1)A = 0.5 \times 0.02 = 0.01 \text{ rad}$
  - ii)  $SS_1 = \text{distance to prism} \times \text{deviation angle} = 0.1 \text{ m} \times 0.01 = 0.001 \text{ m}$    
So  $S_1S_2 = 0.002 \text{ m}$ .
  - iii) Both derived from same source **owtte**
  - iv) fringe width,  $w = L \lambda / S_1S_2 = (1.9+0.1) \times 5 \times 10^{-7} / 0.002 = 5 \times 10^{-4} \text{ m}$

[12 marks]

#### Question 4

- a. A real source with emf 3.0 V and internal resistance 1.0  $\Omega$  is connected to a resistor of resistance 2.0  $\Omega$ .
  - i)  $I = V/R_{\text{circuit}} = 3/3 = 1 \text{ A}$   ;  $V = IR_{2\Omega} = 1 \times 2 = 2 \text{ V}$
  - ii) Net emf =  $3 \text{ V} - 3 \text{ V} = 0$ , thus zero current also
  - iii) By symmetry, or folding over the circuit to superimpose the cells and 1  $\Omega$  resistors, the system has  $E = 3 \text{ V}$ ,  $r = 0.5 \Omega$  connected to 2.5  $\Omega$  load.  $I = V/R = 3 \text{ V} / 3 \Omega = 1 \text{ A}$
  - iv) Now for whole circuit,  $I = V/R = 6 \text{ V} / 2 \Omega = 3 \text{ A}$ .  Consider either cell:  $V_{xy} = \text{zero}$
- b. We will now explore the effect of internal resistance in some practical situations.
  - i) Current through person is  $V/R = 5000 \text{ V} / 10\,001\,000 \approx 0.5 \text{ mA}$  (or potential divider idea, pd across person  $\approx 5 \text{ V}$  leads to  $I = 0.5 \text{ mA}$ )  Therefore harmless (trivial)
  - ii)
    - 1)  $Vit = 12 \text{ V} \times 1 \text{ A} \times (60 \times 3600) \text{ s} = 2.59 \text{ MJ}$
    - 2)  $I = V/R = 12 / 0.01 = 1200 \text{ A}$   ;  $P = V^2/R = 144 / 0.01 = 14.4 \text{ kW}$
    - 3) Heat inside the battery  eventually boils electrolyte with explosion risk or other sensible comment.

[11 marks]

#### Question 5

This question looks at some practical consequences of the evaporation of liquids.

Placing a liquid in a vacuum (e.g. a leak from a space vehicle) forces it to evaporate and can lead to rapid cooling.

- a.  $mc \Delta T = 0.01 \text{ mL}$  hence  $\Delta T = 0.01 \text{ L} / c = .01 \times 2.26 \times 10^6 / 4200 = 5.4^\circ \text{C}$  , new temperature (assuming no other losses) is  $4.6^\circ \text{C}$
- b. All factors lead to rapid evaporation and thus heat loss and sensation of cold **owtte**
- c. Draught enhances evaporation rate. Thus faster cooling **owtte**
- d. More volatile liquids evaporate even faster

[5 marks]